

Directions: Draw a triangle for each problem and then solve (meaning find all solutions/missing parts). If no solutions exist, write none. Round to the nearest tenth.
Hint: You will be using Law of Sines, Ambiguous Case for L.O.S., and Law of Cosines

Write the formulas below

Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

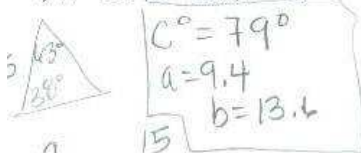
Law of Cosines

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = a^2 + c^2 - 2ac \cos B$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$

1) $A = 38^\circ, B = 63^\circ, c = 15$



$$\frac{a}{\sin 38^\circ} = \frac{15}{\sin 79^\circ}$$

$$a = 9.4$$

$$\frac{b}{\sin 63^\circ} = \frac{15}{\sin 79^\circ}$$

$$b = 13.6$$

3) $a = 12, b = 15, A = 55^\circ$

$$15 \sin 55^\circ < 12 < 15? \\ 12.28 \quad \text{no!}$$

$$\frac{12}{\sin 55^\circ} = \frac{15}{\sin B} \quad \boxed{\text{NO SOL}^n}$$

2) $b = 50, a = 33, A = 132^\circ$

$$\frac{33}{\sin 132^\circ} = \frac{50}{\sin B}$$

$\boxed{\text{NO SOL}^n}$

4) $a = 5, b = 7, c = 10$

$$5^2 = 7^2 + 10^2 - 2(7)(10) \cos A$$

$$-124 = -140 \cos A$$

$$.88 \approx \cos A$$

$$\boxed{27.7^\circ = A}$$

$$\frac{5}{\sin 27.7^\circ} = \frac{7}{\sin B}$$

$$\boxed{40.6^\circ = B}$$

5) $a = 10, c = 8, B = 100^\circ$ L.O.C
 $b^2 = 10^2 + 8^2 - 2(10)(8)\cos 100$
 $b \approx 13.8$
 $\frac{13.8}{\sin 100^\circ} = \frac{10}{\sin A}$
 $A = 45.5^\circ$

$A \approx 45.5^\circ$
 $C = 180 - (100 + 45.5) = 34.5^\circ$
 $b = 13.8$

6) $A = 30^\circ, B = 45^\circ, a = 10$ L.O.S
 $\angle C = 180 - (30 + 45) = 105^\circ$
 $\frac{10}{\sin 30^\circ} = \frac{b}{\sin 45^\circ}$ $\frac{10}{\sin 30^\circ} = \frac{c}{\sin 105^\circ}$
 $14.1 = b$ $19.3 = c$

$b = 14.1$
 $c = 19.3$
 $\angle C = 105^\circ$

Determine the number of possible solutions for each triangle.

7) $A = 42^\circ, a = 22, b = 12$
 $12 \sin 42^\circ < 22 < 12$
 FALSE!
 $\frac{22}{\sin 42^\circ} = \frac{12}{\sin B}$ 1 solⁿ
 $21.4^\circ = B$

8) $a = 15, b = 25, A = 85^\circ$
 $125 \sin 85^\circ < 15 < 25$
 $24.9 < 15 < 25$ FALSE!
 $\frac{15}{\sin 85^\circ} = \frac{25}{\sin B} \rightarrow$ ERROR
NO SOLⁿ

9) $A = 58^\circ, a = 4.5, b = 5$
 $5 \sin 58^\circ < 4.5 < 5$
 $4.2 < 4.5 < 5 \rightarrow$ TRUE!
2 solⁿs

10) $A = 100^\circ, a = 4, c = 4$
 $\downarrow 0$ or 1 solⁿ
 $\frac{4}{\sin 100^\circ} = \frac{4}{\sin C}$
 $80^\circ = C$
1 solⁿ

