

8 I can use previous skills learned as they apply to Chapter 8 topics.

8.1A I can multiply exponential expressions.

Ex 1a: Multiply the following expressions:

a. $5^4 \cdot 5^8$ b. $(3^5)(3)$ c. $x^5 \cdot x^3$
 $5^{12} = 244,140,625$ $3^6 = 729$ x^8

8.1B I can raise exponential expressions to a power.

Ex 1b: Simplify the following expressions:

a. $(b^2)^7$ b. $(-3x)^4$ c. $(3m^7)^4 \cdot m^3$
 b^{14} $(-3)^4 x^4 = 81x^4$ $(3)^4 m^{28} \cdot m^3 = 81m^{31}$

8.1C I can raise a product to a power.

Ex 1c: Simplify the following expressions:

a. $(2 \cdot 3)^3$ b. $(x \cdot y)^8$ c. $(x^2 \cdot u^4)^6$
 $= 2^3 \cdot 3^3$ $x^8 y^8$ $x^{12} u^{24}$
 $= 8 \cdot 27 = 216$

8.1D I can apply the concepts learned to solve word problems.

Ex 1d: You are designing a wall mural that will be composed of squares of different sizes. One of the requirements of your design is that the side length of each square is itself a perfect square.

a. If you represent the side length of a square as x^2 , write an expression for the area of a mural square.

$A = s^2$, if $s = x^2$ then... $A = (x^2)^2 \Rightarrow A = x^4$

b. Find the area of a mural square when $x = 5$

$A = x^4 \Rightarrow A = 5^4 \Rightarrow A = 625 u^2$

8.2A I can divide exponential expressions with the same base.

Ex 2a: Simplify: $\frac{1}{y^6} \cdot y^{15} = \frac{y^{15}}{y^6} = y^{15-6} = y^9$

8.2B I can raise a quotient to a power.

Ex 2b: Simplify each of the following expressions:

a. $\left(\frac{a}{b}\right)^8 = \frac{a^8}{b^8}$ b. $\left(\frac{a^3}{2b^5}\right)^4 = \frac{a^{12}}{2^4 b^{20}} = \frac{a^{12}}{16b^{20}}$ c. $\frac{1}{4x^5} \cdot \left(\frac{2x^2}{y^3}\right)^5 = \frac{1}{4x^5} \cdot \frac{2^5 x^{10}}{y^{15}} = \frac{32x^{10}}{4x^5 y^{15}} = \frac{8x^5}{y^{15}}$

8.2C I can apply the concepts learned to solve word problems

Ex 2b: The distance from the Earth to the nearest galaxy is about 10^{22} meters. The distance from the Earth to the North Star is about 10^{19} meters. How many times further from Earth is the nearest galaxy than the North Star?

$$\frac{10^{22}}{10^{19}} = 10^3 = \boxed{1000}$$

8.3 A I can simplify expressions using exponents that are zero or negative numbers.

Ex 3a: 1. Evaluate each expression:

a. $10^{-3} = \frac{1}{10^3} = \frac{1}{1000}$

b. $\left(\frac{4}{3}\right)^0 = 1$

c. $4^{-6} \cdot 4^3 = \frac{1}{4^3} = \frac{1}{64}$

d. $\frac{1}{5^{-4}} = 5^4 = 625$

2. Simplify each expression:

a. $6y^{-4} = \frac{6}{y^4}$

b. $a^2b^{-4} = \frac{a^2}{b^4}$

c. $(4x^{-3}y^2)^{-3} = 4^3 x^9 y^{-6} = \frac{x^9}{64y^6}$

d. $(8mn^3)^0 = 1$

e. $\frac{x^{-6}}{4y^5} = \frac{1}{4x^6y^5}$

8.3B I can apply the concepts learned to solve word problems

Ex 3b: A hole punch makes holes in your paper that have a diameter of 4^{-1} inch.

a. Write an expression for the area of one punched hole.

Use the formula $A = \pi r^2$

$d = 4^{-1} = \frac{1}{4}$

$r = \frac{1}{4} / 2 = \frac{1}{8}$

$A = \pi \left(\frac{1}{8}\right)^2 \rightarrow A = \frac{\pi}{64}$

b. Your hole punch makes 3 holes in a page. Write an expression for the total area punch out of one sheet of paper.

$A = 3 \left(\frac{\pi}{64}\right) \rightarrow \boxed{A = \frac{3\pi}{64}}$

8.4A I can read and write values in scientific notation.

Ex 4a

a) Write each number in scientific notation: 85.2, 0.00095, 630,000

8.52×10^1 ; 9.5×10^{-4} ; 6.3×10^5

b) Write each number in standard notation: 9.1×10^8 , 4.7×10^{-3} , 6.05×10^2

91,000,000 ; .0047 ; 605

8.4B I can simplify expressions using scientific notations.

Ex 4b: Evaluate each expression:

a. $(5.7 \times 10^3)(2.2 \times 10^{-6})$

12.54×10^{-3}
 1.254×10^{-2}

b. $\frac{6.5 \times 10^{-7}}{1.3 \times 10^{-3}}$

5×10^{-4}
 5.0×10^{-4}

c. $(3 \times 10^{-9})^4$

$3^4 \times (10^{-9})^4$
 81×10^{-36}
 8.1×10^{-35}

8.4C I can compare numbers in standard decimal notation with numbers presented in scientific notation as well as comparing two numbers both of which are presented in scientific notation.

Ex 4c: Order the numbers from least to greatest:

1.305×10^{-3} , 0.000526 , 2.018×10^{-3} , 0.00205
 5.26×10^{-4} 2.05×10^{-3}
 (2) (1) (3) (4)

$.000526$; 1.305×10^{-3} ;
 2.018×10^{-3} ; $.00205$

8.4D I can apply the concepts learned to solve word problems

Ex 4d: Texas has an area of approximately 4.11×10^5 square kilometers. In 2000, the population of Texas was approximately 3.39×10^7 people. How many people were there per square kilometer in Texas in 2000?

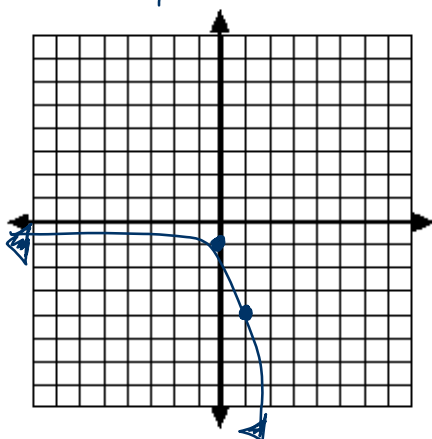
$\frac{3.39 \times 10^7}{4.11 \times 10^5} \approx 0.8248175 \dots \times 10^2$
 $= 8.248 \times 10^1$ people per km^2

8.5A I can write and graph exponential growth models.

Ex 5a: Graph each function and identify its domain and range.

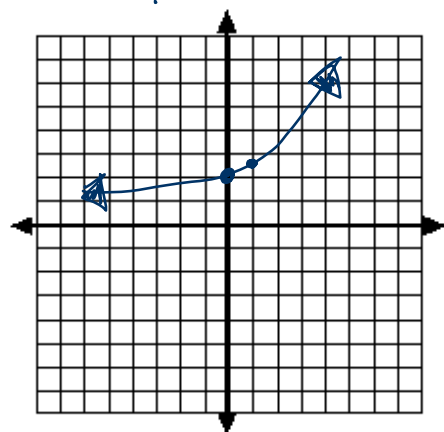
1. $y = -4^x$

$x = 0 \rightarrow -4^0 = -1$, point = $(0, -1)$
 $x = 1 \rightarrow -4^1 = -4$, point = $(1, -4)$
 Domain: All real #'s
 Range: $y < 0$



2. $y = 2 \cdot \left(\frac{4}{3}\right)^x$

$x = 0 \rightarrow 2 \cdot \left(\frac{4}{3}\right)^0 = 2$, point = $(0, 2)$
 $x = 1 \rightarrow 2 \cdot \left(\frac{4}{3}\right)^1 = \frac{8}{3}$, point = $(1, \frac{8}{3})$
 Domain: All real #'s
 Range: $y > 0$



8.5B I can apply the concepts learned to solve word problems.

Ex 5b: You deposit \$200 in a savings account that earns 3% interest compounded yearly.
Find the balance in the account after 5 years.

$$y = a(1+r)^t$$

$$y = 200(1+.03)^5 \rightarrow y = 200(1.15927\dots)$$

$$y = \$231.85$$

8.6A I can write and graph exponential decay models.

Ex 6a: Graph each function.

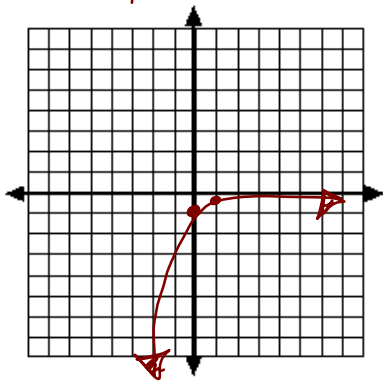
1. $y = -\left(\frac{1}{8}\right)^x$

$x = 0 \rightarrow -\left(\frac{1}{8}\right)^0 = -1$, point = $(0, -1)$

$x = 1 \rightarrow -\left(\frac{1}{8}\right)^1 = -\frac{1}{8}$, point = $(1, -\frac{1}{8})$

Domain: All real #'s

Range: $y < 0$



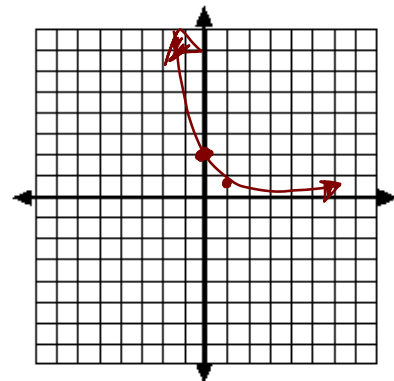
2. $y = 2 \cdot (0.25)^x$

$x = 0 \rightarrow 2 \cdot (0.25)^0 = 2$, point = $(0, 2)$

$x = 1 \rightarrow 2 \cdot (0.25)^1 = \frac{1}{2}$, point = $(1, \frac{1}{2})$

Domain: All real #'s

Range: $y > 0$



8.6B I can use exponential decay models to solve problems.

Ex 6b: A school district bought a bus in 1990 for \$54,000. The value of the tractor has been decreasing at a rate of 3% per year.

a. Use the information to write an exponential decay model

$$y = a(1-r)^t \rightarrow y = 54,000(1-.03)^t \rightarrow y = 54,000(.97)^t$$

b. What was the approximate value of the bus in 1998?

$$y = 54,000(.97)^8 \rightarrow y = 54,000(.783743\dots) \rightarrow y = \$42,322.14$$

8.6C I can distinguish between exponential growth and exponential decay

Ex 6c: For a and b, determine whether each situation is exponential growth or exponential decay - you do not have to solve!

a. You deposit \$5,800 into an account that pays 3% interest compounded annually.

growth

b. A car collector bought a car in 1998 for \$25,000. The value of the car has been decreasing at a rate of 12% per year.

decay